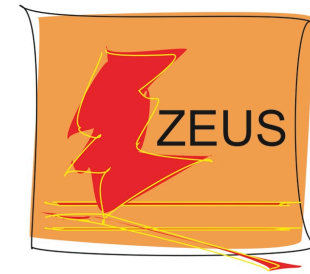


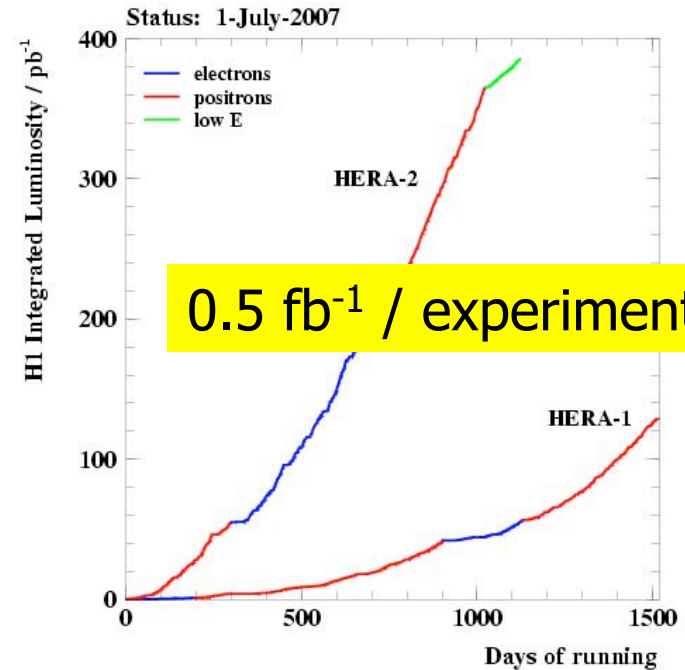
Inclusive high Q^2 cross sections and QCD and EW fits at HERA



Alex Tapper



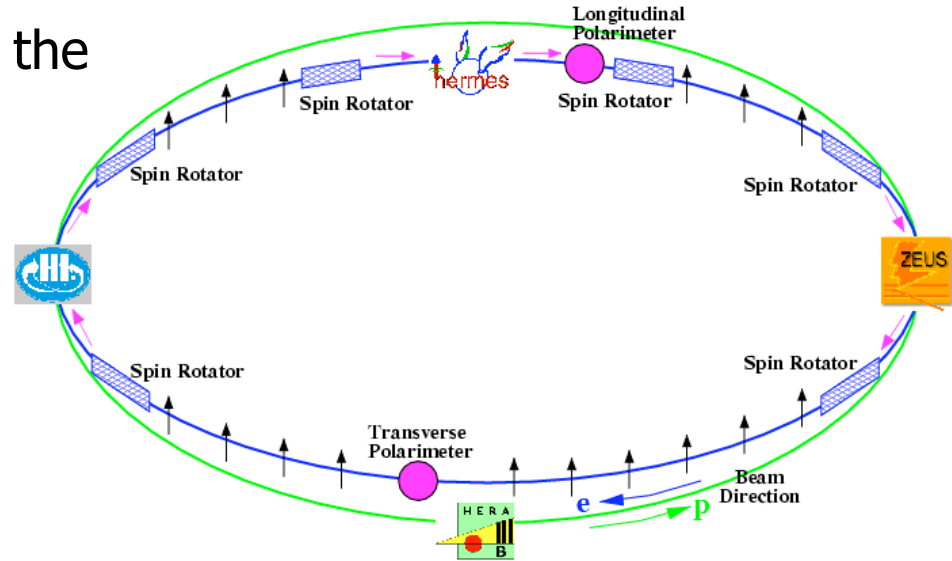
The HERA accelerator



Longitudinal polarisation at HERA

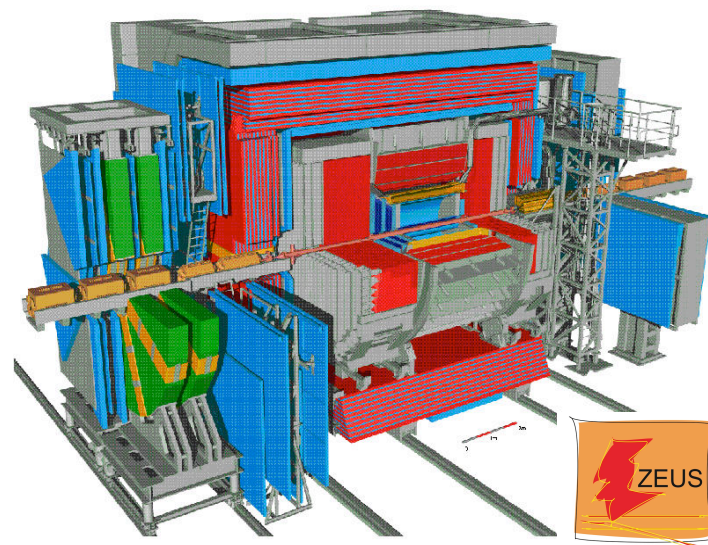
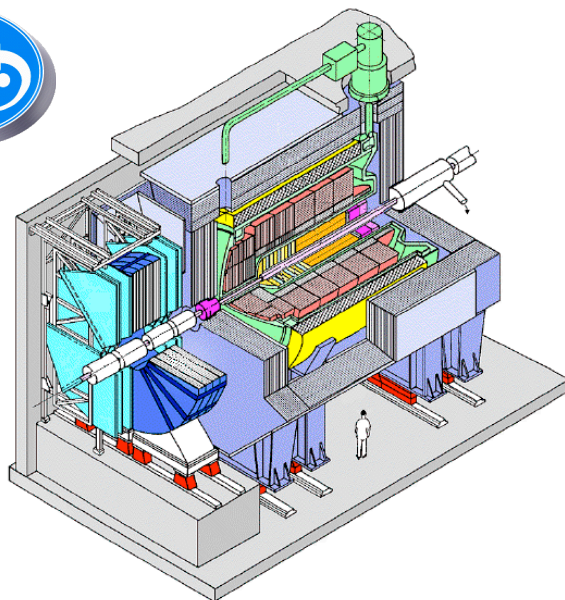
Longitudinal polarisation of the lepton beam at HERA

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$



- Transverse polarisation builds up naturally through synchrotron radiation (Sokolov-Ternov effect)
- Spin rotators flip transverse polarisation to longitudinal before interaction regions and back afterwards
- Polarisation measured by two independent Compton polarimeters
- **Average polarisation 30-40%**

The H1 and ZEUS detectors



- LAr calorimeter (45000 cells)

- EM $\frac{\sigma(E)}{E} = \frac{12\%}{\sqrt{E}} \oplus 1\%$

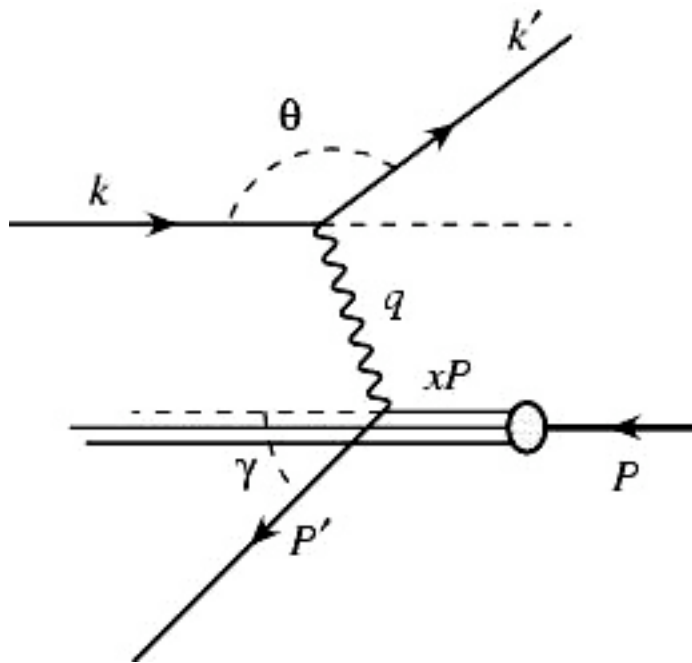
- HAD $\frac{\sigma(E)}{E} = \frac{50\%}{\sqrt{E}} \oplus 1\%$

- DU calorimeter (6000 cells)

- EM $\frac{\sigma(E)}{E} = \frac{18\%}{\sqrt{E}}$

- HAD $\frac{\sigma(E)}{E} = \frac{35\%}{\sqrt{E}}$

Deep inelastic scattering at HERA



Two deep inelastic scattering processes:

- Neutral current: exchange of γ or Z^0
- Charged current: exchange of W^\pm

Q^2 is the probing power
 x is the Bjorken scaling variable
 y is the inelasticity

$$Q^2 = -q^2 = -(k - k')^2$$

$$x = \frac{Q^2}{2p \cdot q} \quad y = \frac{p \cdot q}{p \cdot k}$$

$$s = (p + k)^2 \quad Q^2 = x \cdot y \cdot s$$

Neutral current DIS cross section

$$\frac{d^2 \sigma^{NC}(e^\pm p)}{dx dQ^2} = \frac{2\pi \alpha^2}{x Q^4} Y_+ \left[F_2 - \frac{y^2}{Y_+} F_L \mp \frac{Y_-}{Y_+} xF_3 \right] \quad Y_\pm = 1 \pm (1-y)^2$$

Dominant contribution

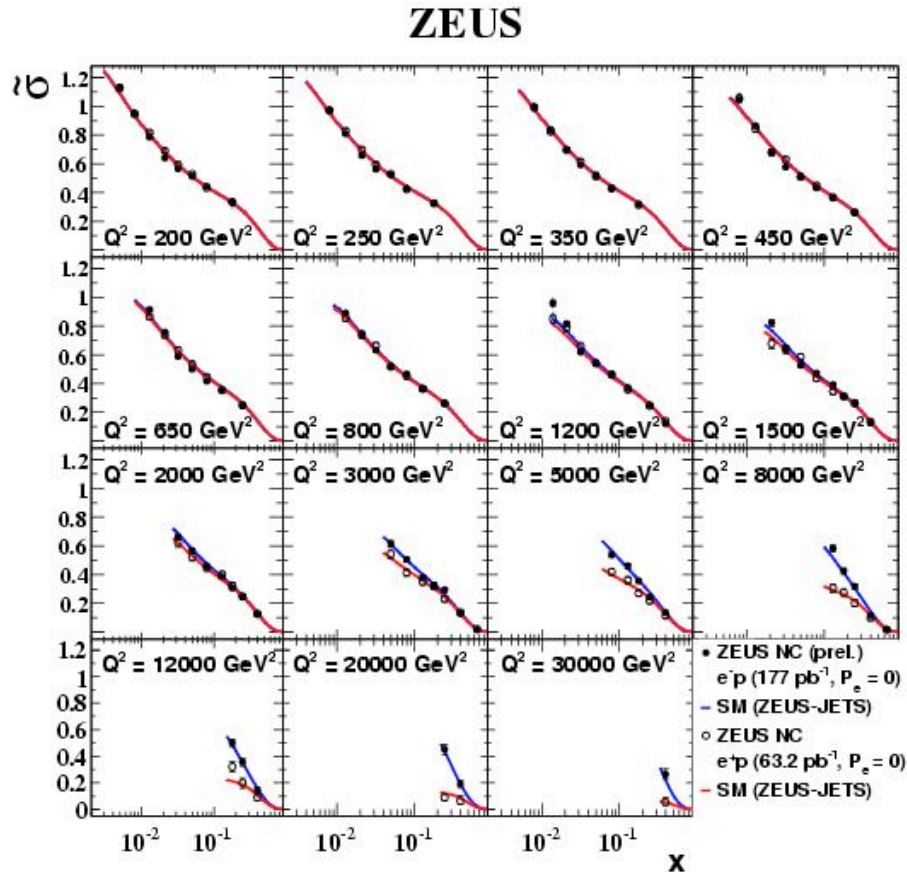
Sizeable only at high y

Contribution only important at high Q^2

$$F_2 = F_2^{em} + \frac{Q^2}{Q^2 + M_Z^2} F_2^{\gamma Z} + \left[\frac{Q^2}{Q^2 + M_Z^2} \right]^2 F_2^Z \propto \sum_{q=u\dots b} (q + \bar{q})$$

$$xF_3 = \frac{Q^2}{Q^2 + M_Z^2} xF_3^{\gamma Z} + \left[\frac{Q^2}{Q^2 + M_Z^2} \right]^2 xF_3^Z \propto \sum_{q=u\dots b} (q - \bar{q})$$

Neutral current data



- At lower Q^2 e^+p and e^-p cross sections the same
 - F_2 (photon exchange) dominates cross section
 - Directly sensitive to sum of quarks and antiquarks

- At high Q^2 e^+p and e^-p cross sections different
 - Influence of xF_3 term (Z^0 exchange)
 - Sensitive to the valence quarks

Charged current DIS at HERA

CC e⁺p cross section:

Sensitive to density of d quark

$$\frac{d^2\sigma^{CC}(e^+p)}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[\underbrace{\bar{u} + \bar{c} + (1-y)^2(d+s)}_{\tilde{\sigma}(x, Q^2)/x} \right]$$

CC e⁻p cross section:

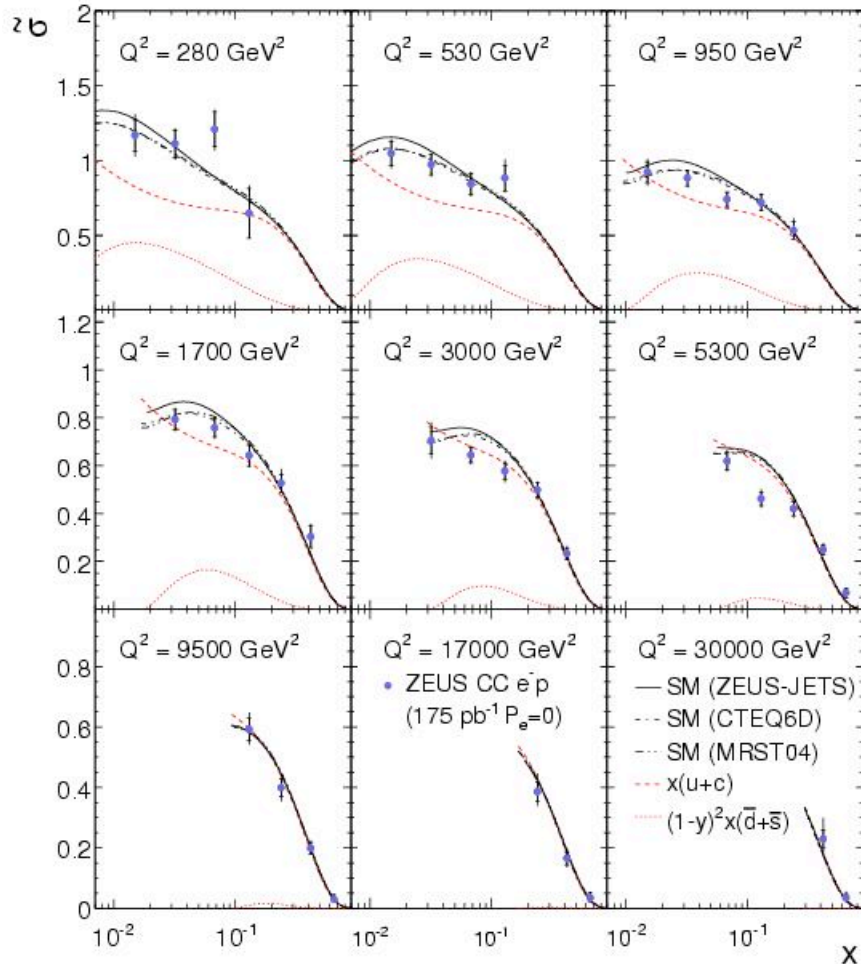
$$\frac{d^2\sigma^{CC}(e^-p)}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[\underbrace{u + c + (1-y)^2(\bar{d} + \bar{s})}_{\tilde{\sigma}(x, Q^2)/x} \right]$$

Sensitive to density of u quark

Electron/positron-proton collisions probe different quark content of proton

Charged current data

ZEUS

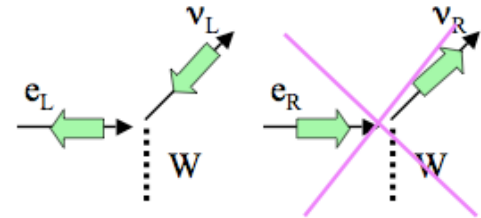


- Charged current cross sections quark-flavour specific
- e^-p (shown here) sensitive to u-quark
- e^+p sensitive to d-quark

Polarised charged current DIS

- Polarisation is asymmetry of helicity states
- Helicity = chirality (neglecting masses)
- Can use polarised beams to directly test chiral structure of the Standard Model
- Standard Model weak interaction left-handed
 - only LH particles (RH anti-particles) interact

$$P_e = \frac{N_R - N_L}{N_R + N_L}$$



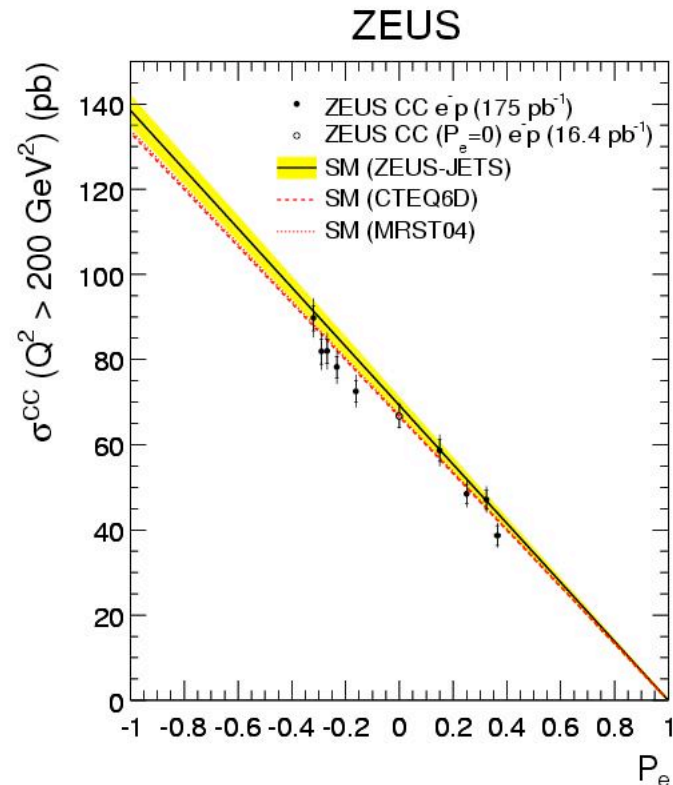
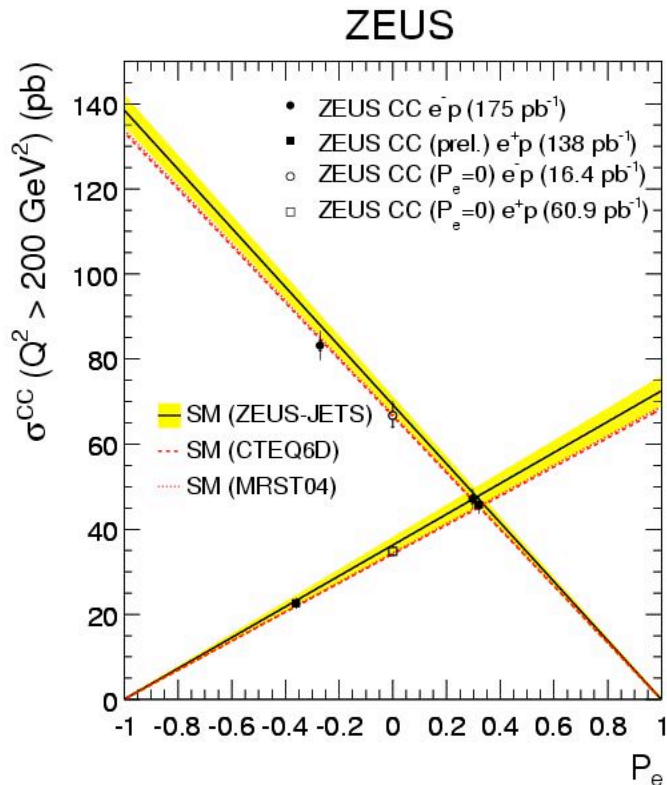
CC cross section modified by P_e :

$$\sigma_{CC}^{e^\pm p}(P_e) = (1 \pm P_e) \cdot \sigma_{CC}^{e^\pm p}(P_e = 0)$$

Polarisation scales $P_e=0$ cross section linearly - **clear and large effect at HERA**

Standard Model predicts zero cross section for $P_e=+1(-1)$ in $e^{(-)(+)}p$ scattering

Dependence on P_e



- Clearly demonstrate linear dependence on P_e
- Consistent with Standard Model predictions

Polarised NC DIS cross sections

NC cross section modified by P:

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[H_0^\pm + PH_P^\pm \right] \quad P = \frac{N_R - N_L}{N_R + N_L}$$

Unpolarised contribution

Polarised contribution - only includes Z and γ Z terms

$$F_2 = \sum_{q=u\dots b} \left(e_q^2 - 2e_q v_q v_e P_Z + (v_e^2 + a_e^2)(v_q^2 + a_q^2) P_Z^2 \right) \cdot x(q + \bar{q})$$

$$xF_3 = \sum_{q=u\dots b} \left(-2e_q a_q a_e P_Z + 4a_q v_q v_e a_e P_Z^2 \right) \cdot x(q - \bar{q})$$

$$P_Z = \frac{1}{\sin^2 \theta_W} \frac{Q^2}{Q^2 + M_Z^2}$$

Polarised NC DIS cross sections

NC cross section modified by P:

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[H_0^\pm + PH_P^\pm \right] \quad P = \frac{N_R - N_L}{N_R + N_L}$$

Unpolarised contribution

Polarised contribution - only includes Z and γ Z terms

$$F_2^P = \sum_{q=u\dots b} \left(2e_q a_e v_q P_Z - 2a_e v_e (v_q^2 + a_q^2) P_Z^2 \right) \cdot x(q + \bar{q})$$

$$xF_3^P = \sum_{q=u\dots b} \left(2e_q a_q v_e P_Z - 2a_q v_q (v_e^2 + a_e^2) P_Z^2 \right) \cdot x(q - \bar{q})$$

$$P_Z = \frac{1}{\sin^2 \theta_W} \frac{Q^2}{Q^2 + M_Z^2}$$

Polarised NC DIS cross sections

NC cross section modified by P:

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[H_0^\pm + PH_P^\pm \right] \quad P = \frac{N_R - N_L}{N_R + N_L}$$

↑
Unpolarised contribution

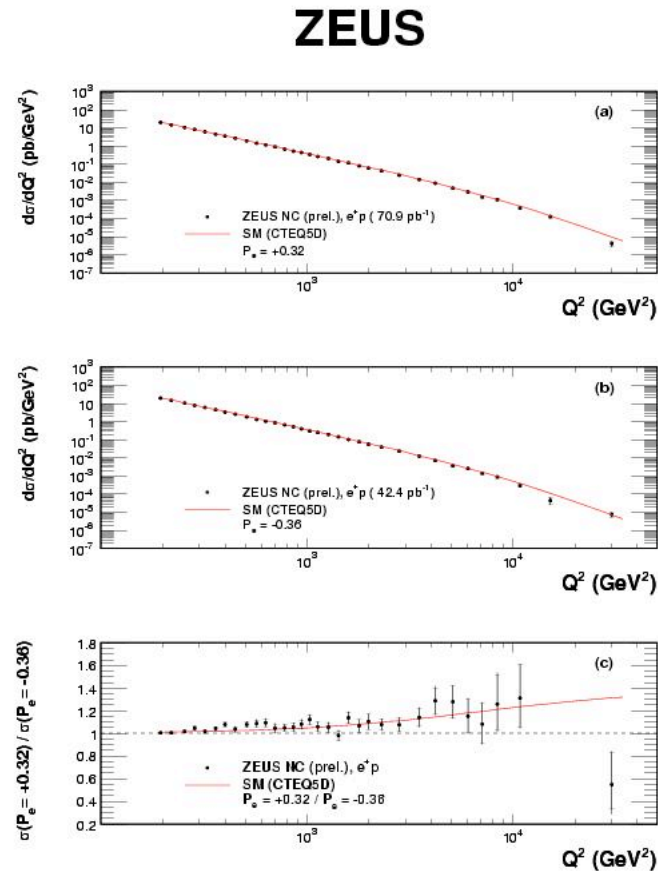
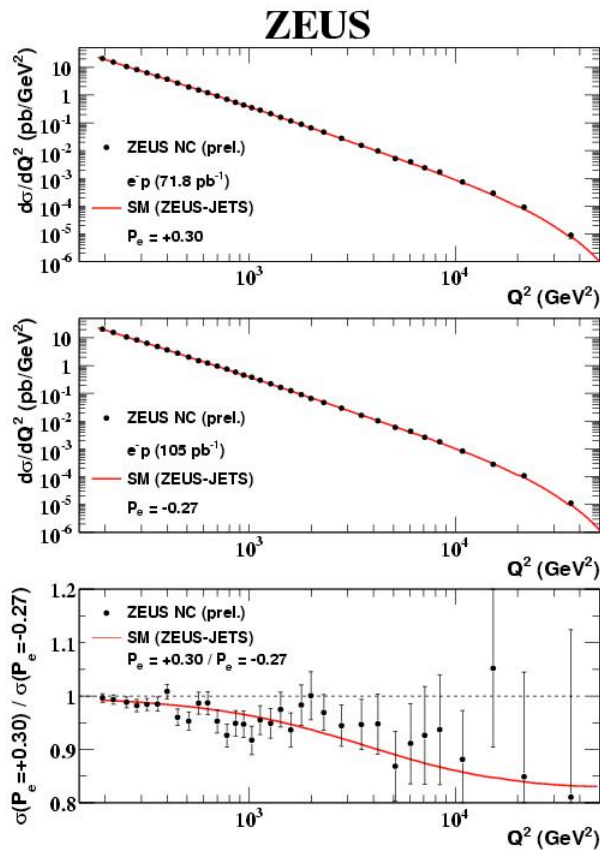
↑
Polarised contribution - only includes Z and γ Z terms

First see if we can observe subtle polarisation dependence!

Then remember that $P_z \gg P_z^2$ and $v_e \sim 0.04$

- Axial couplings from H_0
- Vector couplings from H_P
- u-quark should have best precision (coupling to charge)

Polarised NC measurements



High precision measurements

→ polarisation effect observed

Polarised NC measurements

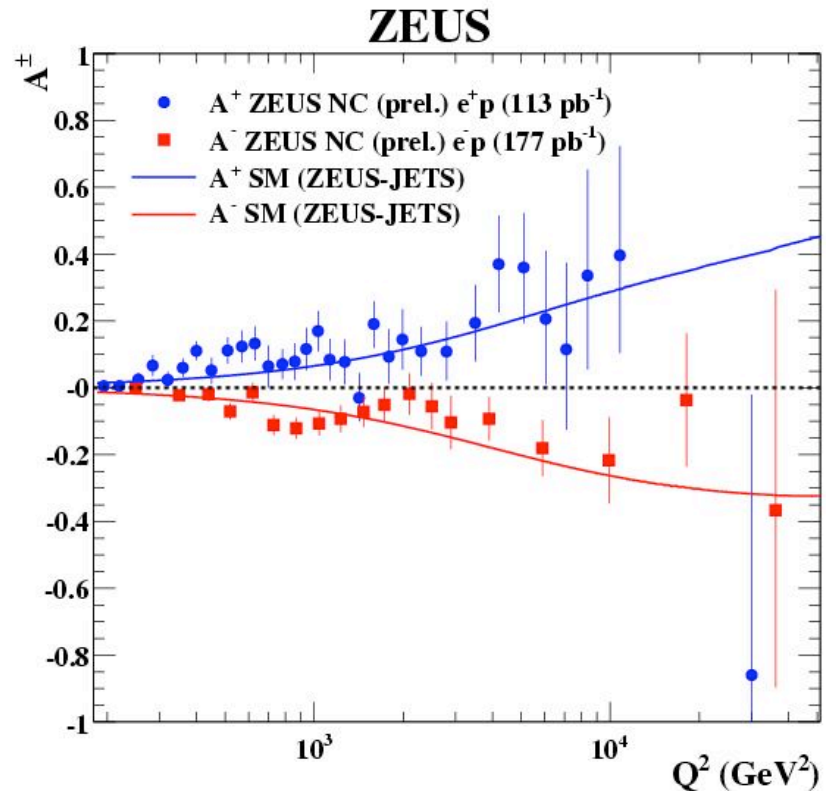
Form the polarisation asymmetry:

$$A^\pm = \frac{2}{P_R - P_L} \frac{\sigma^\pm(P_R) - \sigma^\pm(P_L)}{\sigma^\pm(P_R) + \sigma^\pm(P_L)}$$

to a good approximation

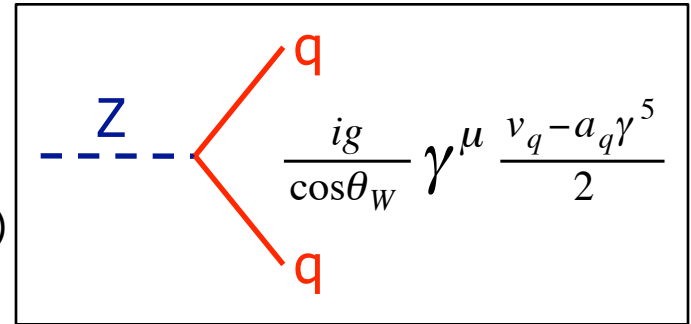
$$A^\pm \approx \mp k a_e \frac{F_2^{\gamma Z}}{F_2} \quad k = \frac{1}{4 \sin^2 \theta_W \cos^2 \theta_W} \frac{Q^2}{Q^2 + M_Z^2}$$

which is quite insensitive to the PDFs and proportional to $a_e v_q$ and therefore a direct measure of parity violation



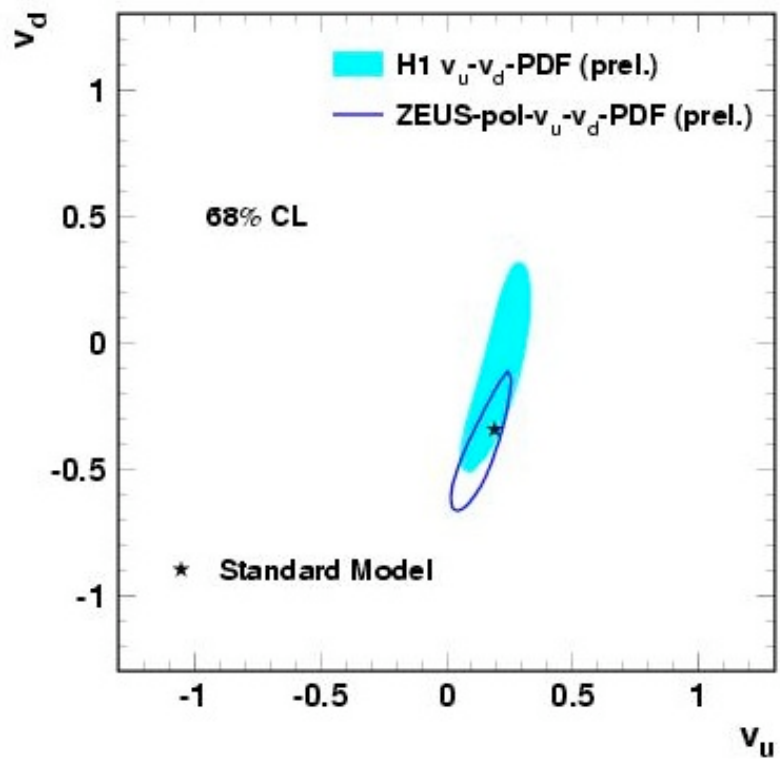
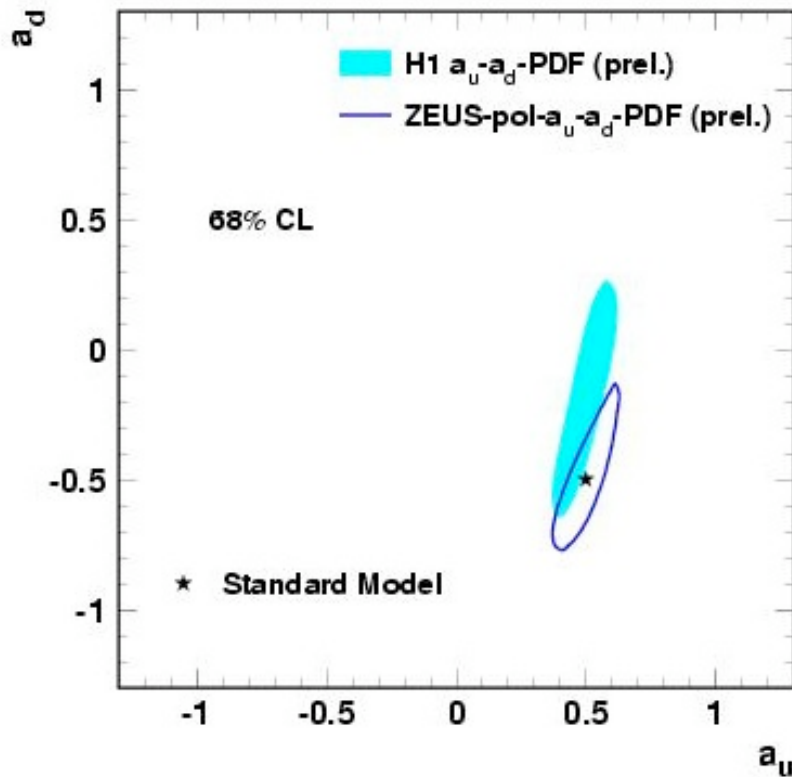
Combined QCD & EW fit

- Simultaneously fit the data for the PDFs and electroweak parameters (Phys. Lett. B 632, 35 (2006))



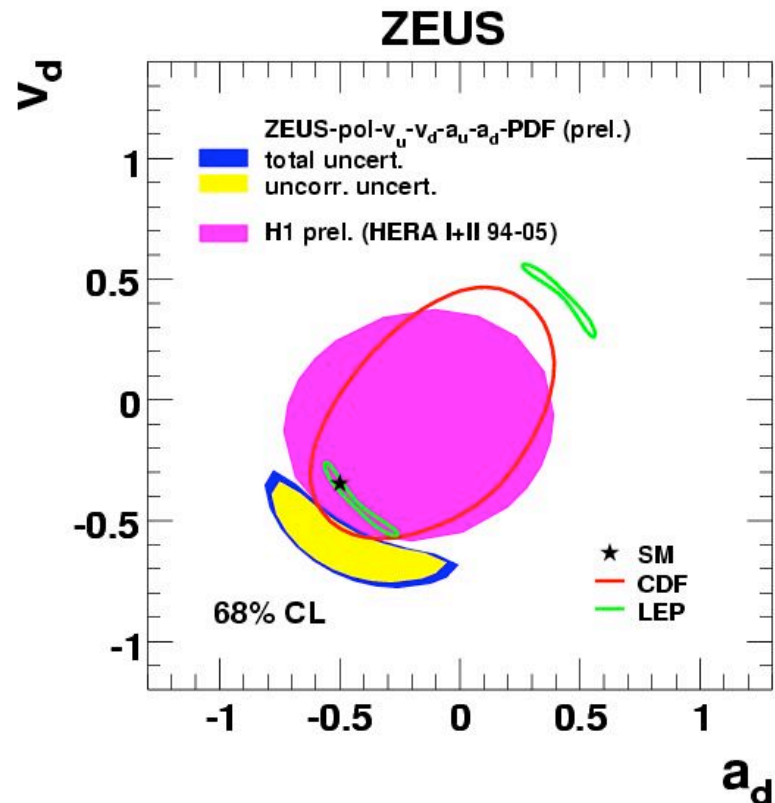
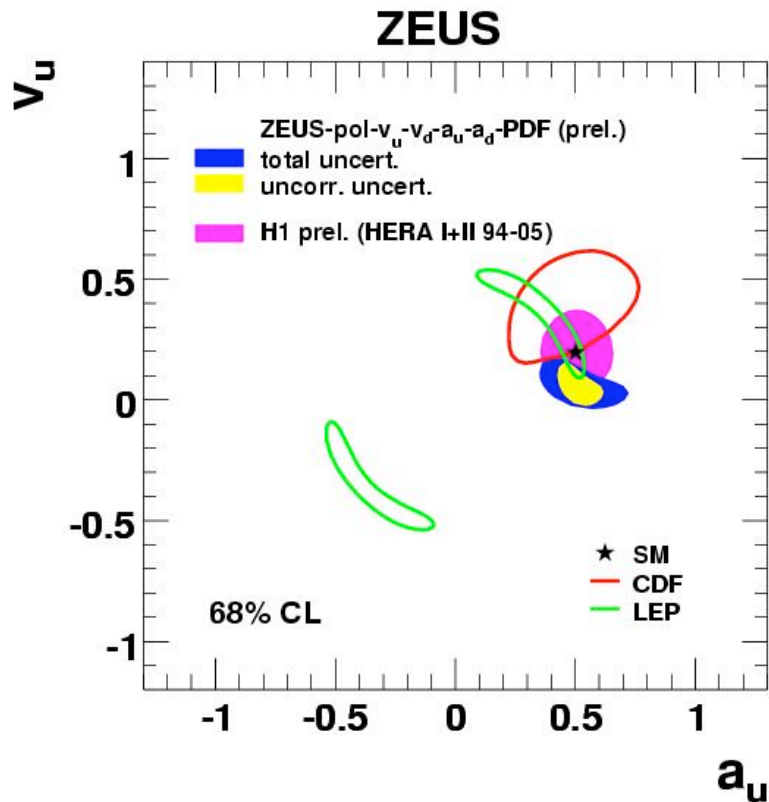
- QCD fits for PDFs well known
 - H1 follows Eur. Phys. J C30 1, (2003).
 - ZEUS follows Eur. Phys. J C42 1, (2005).
 - See talk of Burkard Reisert
- In both cases fits are to H1/ZEUS data only
- For electroweak parameters, exploit the high precision data with longitudinally polarised beams to extract light-quark axial and vector couplings to the Z^0 boson - a_u , a_d , v_u and v_d .

Combined QCD & EW fit



More sensitive to u-quark

Combined QCD & EW fit



HERA measurements competitive with LEP and Tevatron

Phys. Rep. 427, 257 (2006) & Phys. Rev. D71, 052002 (2005)

Summary

- High-precision high- Q^2 measurements
- Simultaneous determinations of the PDFs and EW parameters
- Couplings of u and d quarks to Z^0 competitive with determinations from LEP and Tevatron experiments
- Can expect improvements in precision with full data sets
- Need to combine H1 and ZEUS data
- **More still to come from HERA!**

Backup slides

Electroweak fit

- Fix G_F , M_W in CC cross sections to PDG
- Fix α , M_Z and M_W in NC cross sections to PDG
- $v_q = I_{q,L}^3 - 2e_q \sin^2 \theta_W$ $a_q = I_{q,L}^3$
- Weak radiative corrs modify the couplings to dressed couplings
- Form factors ρ_{eq} , K_e , K_q , K_{eq}
- $\rho_{eq} = 1$ assumed (good up to $Q^2 < 10\,000 \text{ GeV}^2$)
- $\sin^2 \theta_W = \kappa_q (1 - M_W^2/M_Z^2)$

Electroweak fit

ZEUS (prel.) result (H1 numbers not available)

| | a_u | a_d | v_u | v_d |
|------|--------------------------|---------------------------|--------------------------|---------------------------|
| ZEUS | $0.51 \pm 0.10 \pm 0.17$ | $-0.54 \pm 0.32 \pm 0.18$ | $0.05 \pm 0.09 \pm 0.05$ | $-0.64 \pm 0.20 \pm 0.14$ |
| SM | 0.5 | -0.5 | 0.196 | -0.346 |

H1 PDF 2000 fit

- PDFs fitted
 - U, D, Ubar, Dbar and g
- Form
 - $xq(x) = A_q x^{B_q} (1-x)^{C_q} (1 + D_g x + F_q x^3)$
- Starting scale $Q_0^2 = 4 \text{ GeV}^2$
- 10 free parameters for PDFs
- Data sets: NC and CC e^+p and e^-p DIS

ZEUS-JETS fit

- PDFs fitted
 - u and d valence, sea, gluon, $u_{\text{sea}}-d_{\text{sea}}$
- Form
 - $xq(x) = p_1x^{p_2}(1-x)^{p_3}(1+p_4x)$
- Starting scale $Q_0^2=7$ GeV
- 11 free parameters for PDFs
- Data sets: NC and CC e^+p and e^-p DIS, inclusive jets in NC DIS and γp dijets